1. Point $J(p, q)$ is a vertex of quadrilateral $J K L M$. What are the coordinates of $J^{\prime}$ after $J K L M$ is rotated $180^{\circ}$ about the origin?

A $\left({ }^{-} p,{ }^{-} q\right)$

B $\left({ }^{-} p, q\right)$
$\mathrm{C} \quad\left(p,{ }^{-} q\right)$

D $\quad\left(q,{ }^{-} p\right)$
2. $\triangle G H I$ will be dilated by a scale factor of 3 , resulting in $\Delta G^{\prime} H^{\prime} I^{\prime}$.
What rule describes this transformation?

A $\quad\left(x^{\prime}, y^{\prime}\right)=\left(\frac{1}{3} x, \frac{1}{3} y\right)$

B $\quad\left(x^{\prime}, y^{\prime}\right)=(3 x, 3 y)$

C $\quad\left(x^{\prime}, y^{\prime}\right)=(x+3, y+3)$

D $\quad\left(x^{\prime}, y^{\prime}\right)=(x-3, y-3)$
3. $\Delta P^{\prime} Q^{\prime} R^{\prime}$ is the image produced after reflecting $\triangle P Q R$ across the $y$-axis. If vertex $P$ has coordinates ( $s, t$ ), what are the coordinates of $P^{\prime}$ ?

A $\quad(t, s)$
B $\left(s,{ }^{-} t\right)$

C $(-s,-t)$
D $(-s, t)$
4. What is the rule for the transformation formed by a translation 2 units to the left and 3 units up followed by a $90^{\circ}$ counterclockwise rotation?

A $\quad\left(x^{\prime \prime}, y^{\prime \prime}\right)=(-3 y,-2 x)$
B $\quad\left(x^{\prime \prime}, y^{\prime \prime}\right)=(x-2, y+3)$
C $\quad\left(x^{\prime \prime}, y^{\prime \prime}\right)=[-(y+3), x-2]$
D $\quad\left(x^{\prime \prime}, y^{\prime \prime}\right)=[-(y-2), x+3]$
5. The point $G(2,-7)$ is transformed according to the rule $\left(x^{\prime}, y^{\prime}\right)=(x+2, y-3)$. The image $G^{\prime}$ of the transformation is then reflected over the line $y=x$, resulting in point $G^{\prime \prime}$. What are the coordinates of $G^{\prime \prime}$ ?

A $(4,10)$
B $\left(4,{ }^{-1} 10\right)$

C $\quad(-10,4)$

D $\quad(-4,10)$
6. $\Delta G^{\prime} H^{\prime} I^{\prime}$ is the image of $\Delta G H I$ after a transformation.


Which choice describes the transformation shown?
A reflection over $x$-axis
B reflection over $y$-axis
C $\quad\left(x^{\prime}, y^{\prime}\right)=(x-8, y)$
D $\quad\left(x^{\prime}, y^{\prime}\right)=(x, y-8)$
7. Point $J(p, q)$ is a vertex of $\triangle J K L$. What are the coordinates of $J^{\prime}$ after $\triangle J K L$ is reflected across the line $y=x$ ?

A $\left({ }^{-} p,{ }^{-} q\right)$
B $(p,-q)$
C $\left(q,{ }^{-} p\right)$
D $(q, p)$
8. $\triangle X Y Z$ is dilated by a factor of $\frac{1}{2}$. What is the ratio of the area of $\triangle X Y Z$ to the area of its image, $\Delta X^{\prime} Y^{\prime} Z^{\prime}$ ?

A $4: 1$
B $2: 1$
C $1: 2$
D $1: 4$
9. $\triangle D E F$ is reflected across the line $y=x$.


Which matrix multiplication shows how to find $\Delta D^{\prime} E^{\prime} F^{\prime}$ ?
A $\left[\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right]\left[\begin{array}{lll}4 & 5 & 6 \\ 1 & 3 & 1\end{array}\right]$
B $\left[\begin{array}{ll}0 & 1 \\ 1 & 0\end{array}\right]\left[\begin{array}{lll}4 & 5 & 6 \\ 1 & 3 & 1\end{array}\right]$
C $\quad\left[\begin{array}{rr}-1 & 0 \\ 0 & -1\end{array}\right]\left[\begin{array}{lll}4 & 5 & 6 \\ 1 & 3 & 1\end{array}\right]$
D $\left[\begin{array}{rr}0 & -1 \\ -1 & 0\end{array}\right]\left[\begin{array}{lll}4 & 5 & 6 \\ 1 & 3 & 1\end{array}\right]$
10. Triangle $M R T$ has vertices at $M(3,8), R\left(7,{ }^{-} 2\right)$, and $T\left({ }^{-} 5,{ }^{-} 4\right)$. If the triangle is to be translated by the rule $\left(x^{\prime}, y^{\prime}\right)=(x+3, y-2)$, which matrix expression models the translation?

A $\quad\left[\begin{array}{rrr}3 & 7 & -5 \\ 8 & -2 & -4\end{array}\right]+\left[\begin{array}{rrr}3 & 3 & 3 \\ -2 & -2 & -2\end{array}\right]$
B $\left[\begin{array}{rrr}3 & 7 & -5 \\ 8 & -2 & -4\end{array}\right]-\left[\begin{array}{rrr}-2 & -2 & -2 \\ 3 & 3 & 3\end{array}\right]$
C $\left[\begin{array}{rrr}3 & 7 & -5 \\ 8 & -2 & -4\end{array}\right]+\left[\begin{array}{rrr}-2 & -2 & -2 \\ 3 & 3 & 3\end{array}\right]$
D $\left[\begin{array}{rrr}3 & 7 & -5 \\ 8 & -2 & -4\end{array}\right]-\left[\begin{array}{rrr}3 & 3 & 3 \\ -2 & -2 & -2\end{array}\right]$
11. Which matrix calculation was used to transform $\triangle S T U$ to $\Delta S^{\prime} T^{\prime} U^{\prime}$ ?


A $\left[\begin{array}{rr}0 & -1 \\ 1 & 0\end{array}\right]\left[\begin{array}{rrr}-7 & -4 & -3 \\ 0 & 2 & 8\end{array}\right]$
B $\left[\begin{array}{rr}-1 & 0 \\ 0 & -1\end{array}\right]\left[\begin{array}{rrr}-7 & -4 & -3 \\ 0 & 2 & 8\end{array}\right]$
C $\left[\begin{array}{rr}-1 & 0 \\ 0 & 1\end{array}\right]\left[\begin{array}{rrr}-7 & -4 & -3 \\ 0 & 2 & 8\end{array}\right]$
D $\left[\begin{array}{rr}0 & -1 \\ -1 & 0\end{array}\right]\left[\begin{array}{rrr}-7 & -4 & -3 \\ 0 & 2 & 8\end{array}\right]$
12. $\triangle G H J$ with vertex matrix $\left[\begin{array}{rrr}-2 & 3 & 3 \\ 4 & 6 & -2\end{array}\right]$ is dilated by a factor of $\frac{1}{3}$. In the image $\Delta G^{\prime} H^{\prime} J^{\prime}$, what are the coordinates of the vertex that lies in the second quadrant?

A $\left(-\frac{7}{3}, \frac{13}{3}\right)$

B $\quad\left(-\frac{2}{3}, \frac{4}{3}\right)$

C $\quad\left(1,-\frac{2}{3}\right)$

D $(1,2)$
13. The vertices of quadrilateral GHIJ are $G\left({ }^{-} 1,{ }^{-} 1\right), H\left(3,{ }^{-} 2\right), I(2,4)$, and $J\left({ }^{-} 2,3\right)$. $G^{\prime} H^{\prime} I^{\prime} J^{\prime}$ is the image produced by translating quadrilateral GHIJ 6 units to the left. Which matrix represents $G^{\prime} H^{\prime} I^{\prime} J^{\prime}$ ?

A $\left[\begin{array}{cccc}-7 & -3 & -4 & -8 \\ -7 & -8 & -2 & -3\end{array}\right]$
B $\left[\begin{array}{rrrr}-7 & -3 & -4 & -8 \\ -1 & -2 & 4 & 3\end{array}\right]$
C $\left[\begin{array}{rrrr}-1 & 3 & 2 & -2 \\ -7 & -8 & -2 & -3\end{array}\right]$
D $\left[\begin{array}{rrrr}5 & 9 & 8 & 4 \\ -1 & -2 & 4 & 3\end{array}\right]$
14. $\Delta M^{\prime} N^{\prime} O^{\prime}$ is the image of $\triangle M N O$ produced by a translation 3 units left and 1 unit up. The vertex matrix for $\triangle M^{\prime} N^{\prime} O^{\prime}$ is $\left[\begin{array}{rrr}-1 & 2 & 4 \\ 1 & 6 & -3\end{array}\right]$. Which is the vertex matrix for $\triangle M N O$ ?

A $\left[\begin{array}{rrr}2 & 5 & 7 \\ 0 & 5 & -4\end{array}\right]$
B $\left[\begin{array}{rrr}-4 & -1 & 1 \\ 2 & 7 & -2\end{array}\right]$
C $\quad\left[\begin{array}{rrr}- \\ 2 & 1 & 3 \\ 4 & 9 & 0\end{array}\right]$
D $\left[\begin{array}{rrr}0 & 3 & 5 \\ -2 & 3 & -6\end{array}\right]$
15. Polygon $F G H I$ is represented by vertex matrix $M$.

$$
M=\left[\begin{array}{rrrr}
2 & 4 & 4 & 2 \\
-2 & -2 & -5 & -5
\end{array}\right]
$$

Which multiplication would be used to reflect polygon $F G H I$ across the $x$-axis?
A $\left[\begin{array}{rr}1 & 0 \\ 0 & -1\end{array}\right]\left[\begin{array}{rrrr}2 & 4 & 4 & 2 \\ -2 & -2 & -5 & -5\end{array}\right]$
B $\left[\begin{array}{rr}-1 & 0 \\ 0 & 1\end{array}\right]\left[\begin{array}{rrrr}2 & 4 & 4 & 2 \\ -2 & -2 & -5 & -5\end{array}\right]$
C $\left[\begin{array}{rr}-1 & 0 \\ 0 & -1\end{array}\right]\left[\begin{array}{rrrr}2 & 4 & 4 & 2 \\ -2 & -2 & -5 & -5\end{array}\right]$
D $\left[\begin{array}{rr}0 & -1 \\ -1 & 0\end{array}\right]\left[\begin{array}{rrrr}2 & 4 & 4 & 2 \\ -2 & -2 & -5 & -5\end{array}\right]$

## End of Goal 3 Sample Items

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6 Objective:
Describe the transformation (translation, reflection, rotation, dilation) of polygons in the coordinate plane in simple algebraic terms.
Thinking Skill: Analyzing Correct Answer: D

## Objective: <br> 3.01

Describe the transformation (translation, reflection, rotation, dilation) of polygons in the coordinate plane in simple algebraic terms.
Thinking Skill: Applying Correct Answer: D
Objective: $\quad 3.01$
Describe the transformation (translation, reflection, rotation, dilation) of polygons in the coordinate plane in simple algebraic terms.
Thinking Skill: Analyzing Correct Answer: A

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Objective: 3.02
Use matrix operations (addition, subtraction, multiplication, scalar multiplication) to describe the transformation of polygons in the coordinate plane.
Thinking Skill:
Applying
Correct Answer: A

